

TIME 2014.



The task we do, the software we choose

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Some years ago in teaching of mathematics we have Dynamic Geometry Software (DGS) that offer some options in the design of teaching-learning activities.

We could choose the software according to the task and its objectives.

This is so because the construction philosophy is different for each application, and thus the knowledge they foster.

Today, the trend is that, in a few years, only one of such applications will be at hand, and the only reason is that it is for free.

We stand that there is not a DGS application better than the other, their use should depend on the task at hand and the learning objectives we want to achieve.

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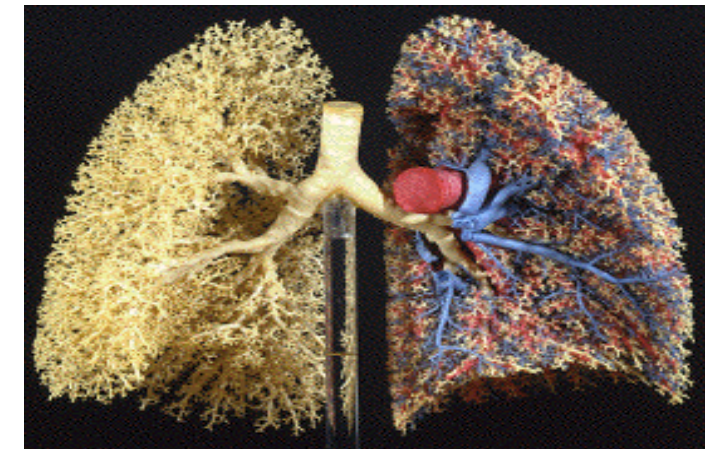
**We will make our point comparing two
DGS in a fractal construction activity:**

**GeoGebra and The Geometer's
Sketchpad.**

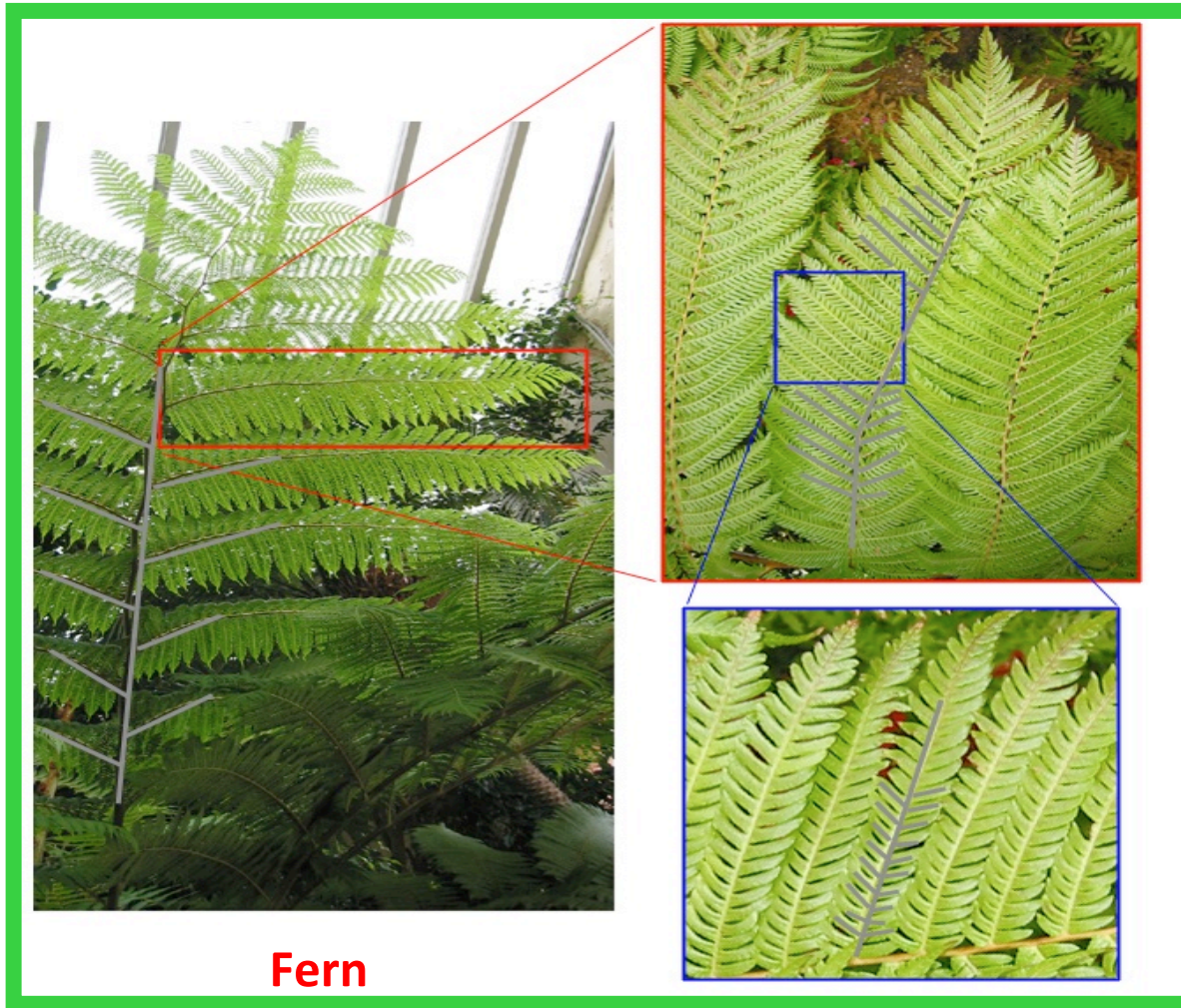
Time 2014. Similarity Property



Kidney



Lungs



Fern

(Benoit Mandelbrot, 1970's)

“Fractal” means: fragmented. A lot of pieces.
Fractional dimension

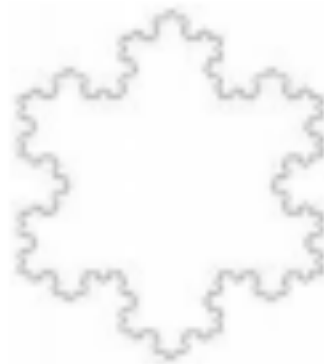


Example: Perimeter

$$\text{Dim}_{\text{Fractal}} = 1.2619\dots$$

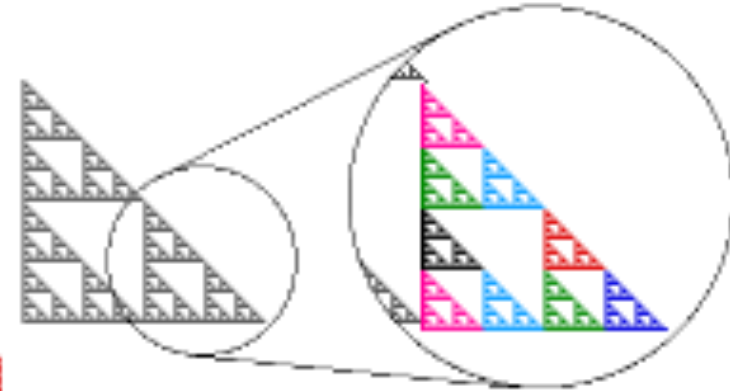
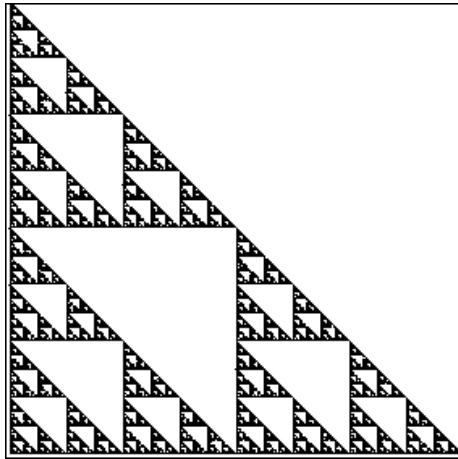
$$\text{Dim}_{\text{Topologica}} = 1$$

$$\therefore \text{Dim}_{\text{Fractal}} > \text{Dim}_{\text{Topologica}}$$



$$D_F = \frac{\ln \eta}{\ln \frac{1}{r}}$$





It does made of little copies of itself

$$\eta r^D = 1$$

Power law



TIME 2014. How usually does the fractal is defined?

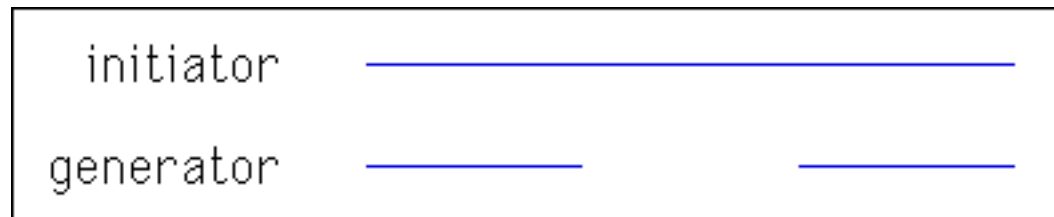


It is defined as a limit of an iterative process

- 1) Start with a initiator
- 2) Give a rule (usually DELETE a part of the initiator and substitute for another)
- 3) Iterate as much as possible, and....

These iterations give a sequence of shapes converging to a fractal!

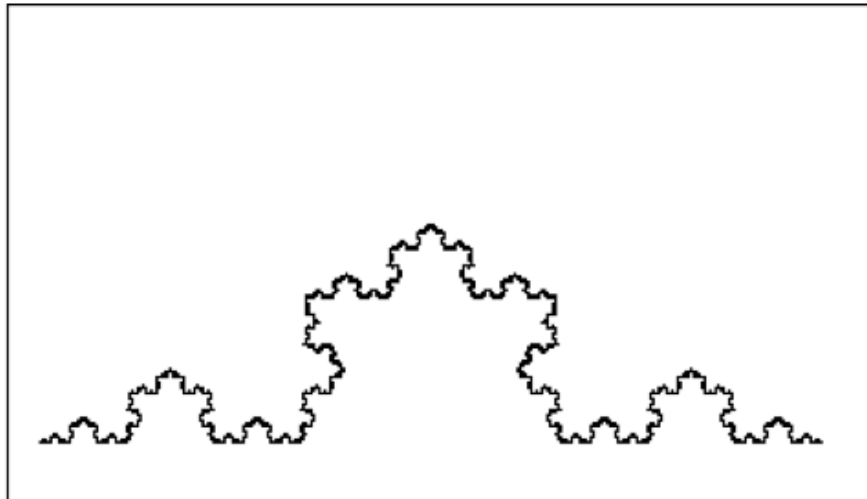
In other words: the limit curve is a fractal → INFINITUM



Cantor dust

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Koch Curve



Helge Von Koch

1870-1924

koch-mejorado.ggb

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Vista Algebraica Vista Gráfica

Cónica

- c1: $(x + 4)^2 + y^2 = 7.11$
- c2: $(x - 4)^2 + y^2 = 7.11$
- c₃: $(x + 3.07)^2 + (y - 7.96)^2 =$
- c₄: $(x - 0.49)^2 + (y - 9.5)^2 =$
- c₅: $(x + 3.66)^2 + (y - 7.96)^2 =$
- c₆: $(x + 2.18)^2 + (y - 7.96)^2 =$
- c₇: $(x + 1.29)^2 + (y - 7.96)^2 =$
- c₈: $(x + 0.7)^2 + (y - 9.5)^2 =$
- c₁₂: $(x - 3.45)^2 + (y - 7.96)^2 =$
- d1: $(x + 1.33)^2 + y^2 = 7.11$
- d2: $(x - 1.33)^2 + y^2 = 7.11$
- d₂: $(x - 2.22)^2 + (y - 4)^2 =$
- d₃: $(x + 1.29)^2 + (y - 7.96)^2 =$
- d₄: $(x - 1.37)^2 + (y - 7.96)^2 =$
- d₅: $(x + 3.07)^2 + (y - 7.96)^2 =$
- d₆: $(x + 2.63)^2 + (y - 8.73)^2 =$
- d₇: $(x + 1)^2 + (y - 8.47)^2 =$
- d₁₁: $(x - 2.41)^2 + (y - 8.22)^2 =$
- d₁₂: $(x - 4.04)^2 + (y - 7.96)^2 =$
- e₁: $(x + 0.89)^2 + (y - 4.77)^2 =$
- e₂: $(x - 4)^2 + (y - 4)^2 = 0.79$
- e₃: $(x + 3.96)^2 + (y - 7.96)^2 =$
- e₄: $(x - 0.04)^2 + (y - 10.27)^2 =$
- e₅: $(x + 3.96)^2 + (y - 7.96)^2 =$
- e₆: $(x + 2.33)^2 + (y - 8.22)^2 =$

Entrada:

Step 3

Step 2

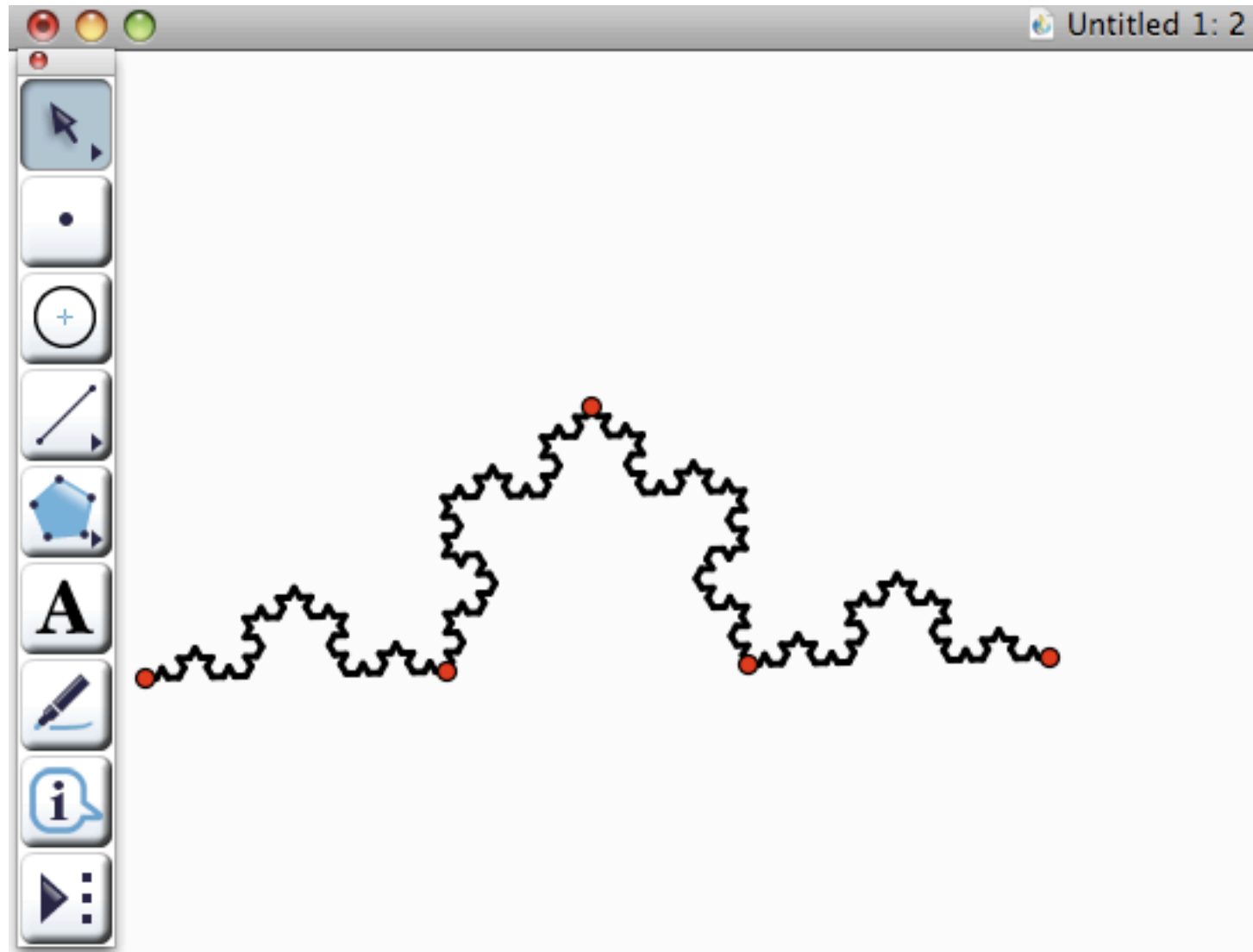
Step 1

Algorithm

Step 0

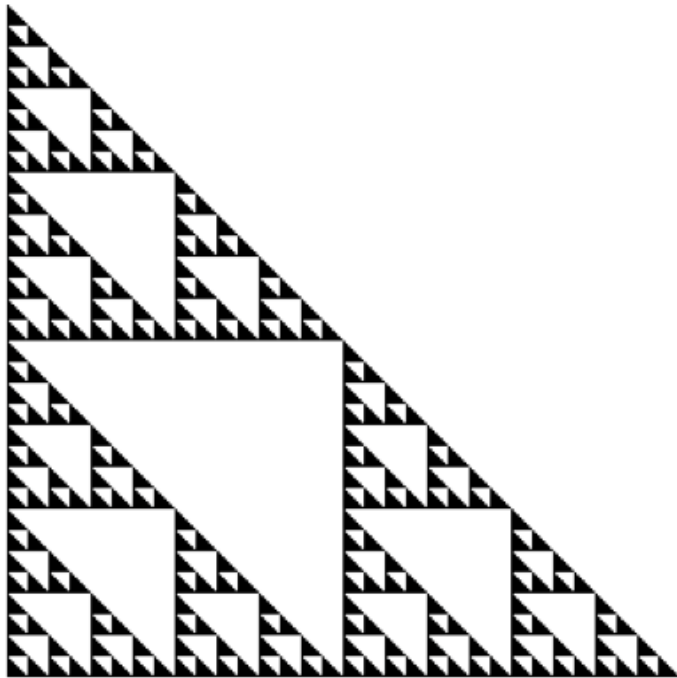
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Sketchpad



Wacław Sierpiński

1882-1969



TS-SET.ggb

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Elige y Mueve: Enmarcado o selección, uno a uno (Ctrl), de objetos (Esc para salir)

Vista Algebraica

Lista

- $A1 = \{(0, 0), (10, 0), (5, 8.66)\}$
- $A2 = \{(0, 0), (5, 0), (2.5, 4.33)\}, \{(10, 0), (5, 0), (7.5, 4.33)\}$
- $A3 = \{(0, 0), (2.5, 0), (1.25, 2.17)\}, \{(5, 0), (2.5, 0), (3.75, 2.17)\}, \{(10, 0), (7.5, 0), (8.75, 2.17)\}$
- $B2 = \{10.83, 10.83, 10.83\}$
- $B3 = \{2.71, 2.71, 2.71, 2.71, 2.71, 2.71, 2.71, 2.71, 2.71\}$

Número

- $n = 7$

Punto

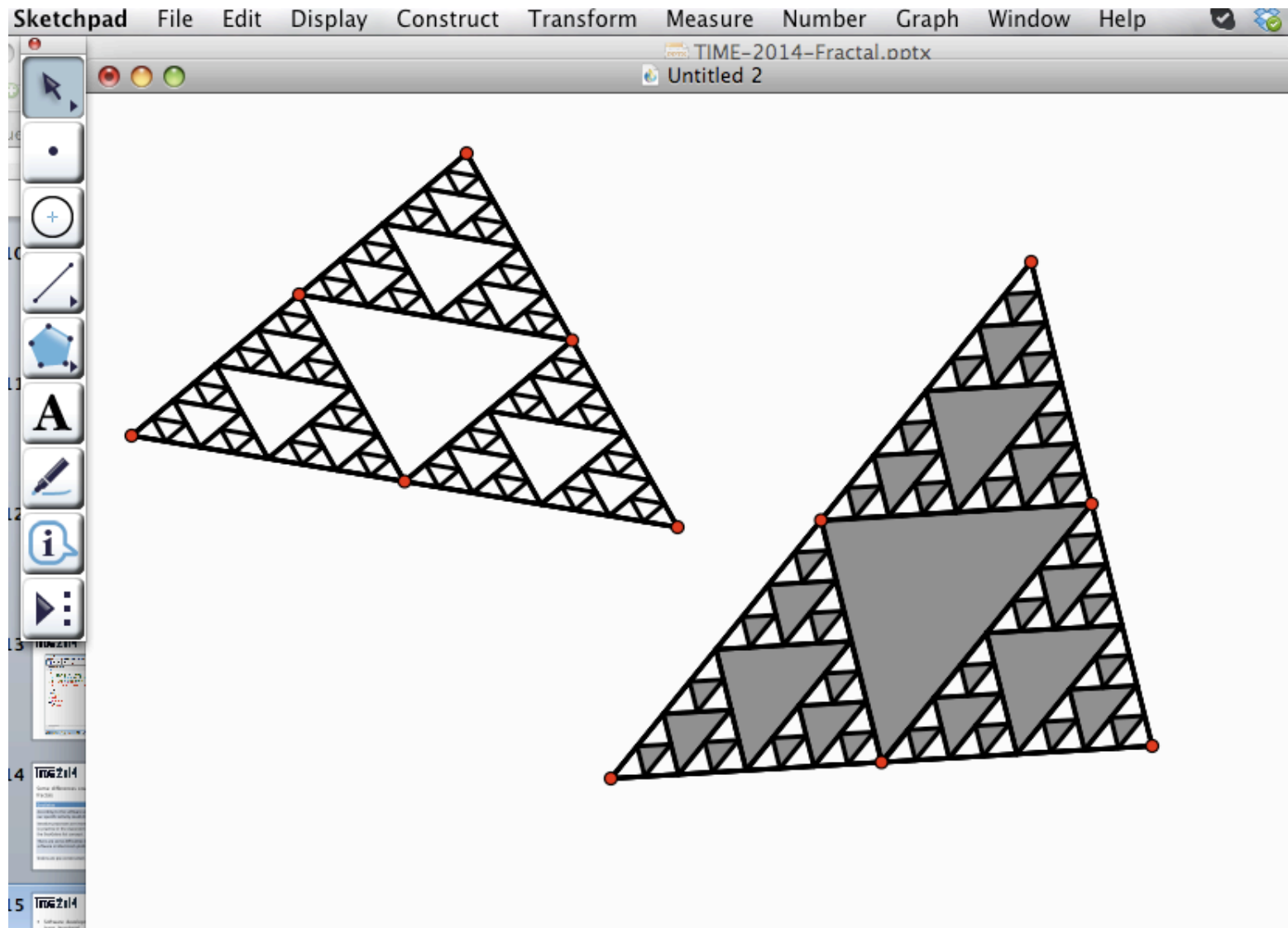
- $A = (0, 0)$
- $B = (10, 0)$
- $C = (5, 8.66)$

Triángulo

- $B1 = 43.3$

Vista Gráfica

Entrada:



Some differences could be detected in order to construct fractals

GeoGebra	Sketchpad
According to the software version our specific activity could change.	Despite the software version the activity does not change.
Iterative processes are more difficult to practice in the classroom without the GeoGebra list concept.	It is easier to get the idea of iterative process in the classroom.
There are some difficulties to run the software in Macintosh platform.	There is not problem in running the software in either Macintosh or a PC platforms.
Sliders are pre-constructed.	Slider have to be constructed.

- Software development goes much faster than we can learn (teachers) → There are some useful attributes that are lost in each transition.
- In the classroom, Sketchpad permits a more effective approach of, for instance,
 - ✓ Pattern searching
 - ✓ Review of the infinitum concept

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Danke schön
Thank you
Gracias